

SIGNATURE \_\_\_\_\_ NAME \_\_\_\_\_

Student ID # \_\_\_\_\_

**Physics 410**  
**Spring 2013**  
**Prof. Anlage**  
**First Mid-Term Exam**  
**1 March, 2013**  
**CLOSED BOOK, Calculator Permitted, CLOSED NOTES**

**Point totals are given for each part of the question.**

If you run out of room, continue writing on the back of the same page. If you do so,  
 make a note on the front part of the page!

Note: You must solve the problem following the instructions given in the problem.  
 Correct answers alone will not receive full credit.

**Partial Credit:**

→ Show Your Work! Answers written with no explanation will not receive full credit.

→ You can receive credit for describing the method you would use to solve a problem, even if you missed an earlier part.

Problem	Credit	Max. Credit
1		25
2		25
3		20
4		30
TOTAL		100

$$\vec{r} \cdot \vec{s} = rs \cos \theta \quad \vec{r} \times \vec{s} = \det \begin{bmatrix} \hat{x} & \hat{y} & \hat{z} \\ r_x & r_y & r_z \\ s_x & s_y & s_z \end{bmatrix} \quad \vec{F} = m\ddot{\vec{r}} \quad \vec{f} = -f(v)\hat{v} \quad f(v) = bv + cv^2$$

$$\vec{F} = q(\vec{E} + \vec{v} \times \vec{B}) \quad m\dot{v} = -\dot{m}v_{ex} + F^{ext} \quad v - v_0 = v_{ex} \ln \frac{m_0}{m} \quad \vec{R} = \frac{1}{M} \sum_{\alpha=1}^N m_{\alpha} \vec{r}_{\alpha}$$

$$\vec{\ell} = \vec{r} \times \vec{p} \quad \vec{L} = \frac{1}{M} \sum_{\alpha=1}^N \vec{r}_{\alpha} \times \vec{p}_{\alpha} \quad \dot{\vec{L}} = \vec{\Gamma}^{ext} \quad \Delta T = T_2 - T_1 = \int_1^2 \vec{F} \cdot d\vec{r} = W(1 \rightarrow 2)$$

$$T = mv^2/2 \quad U(\vec{r}) = -W(\vec{r}_0 \rightarrow \vec{r}) = -\int_{\vec{r}_0}^{\vec{r}} \vec{F}(\vec{r}') \cdot d\vec{r}' \quad \vec{\nabla} \times \vec{F} = 0 \quad \vec{F} = -\vec{\nabla} U$$

$$E = T + U_1 + \dots + U_n \quad \Delta E = W_{nc} \quad t = \sqrt{\frac{m}{2}} \int_{x_0}^x \frac{dx'}{\sqrt{E - U(x')}} \quad \vec{F}(\vec{r}) = f(\vec{r})\hat{r} \quad U = U^{int} + U^{ext}$$

$$U^{ext} = \sum_{\alpha} \sum_{\beta > \alpha} U_{\alpha\beta} + \sum_{\alpha} U_{\alpha}^{ext} \quad \text{Net force on particle } \alpha = -\nabla_{\alpha} U \quad T + U = \text{constant}$$

$$F = -kx \leftrightarrow U = \frac{1}{2} kx^2 \quad \ddot{x} = -\omega^2 x \leftrightarrow x(t) = A \cos(\omega t - \delta) \quad \ddot{x} + 2\beta\dot{x} + \omega_0^2 x = 0 \leftrightarrow x(t) = Ae^{-\beta t} \cos(\omega_1 t - \delta) \quad (\text{assuming } \beta < \omega_0), \beta = \frac{2b}{m}, \text{damping force} =$$

$$-bv, \omega_0 = \sqrt{\frac{k}{m}}, \omega_1 = \sqrt{\omega_0^2 - \beta^2} \quad F(t) = mf_0 \cos(\omega t), x(t) = A \cos(\omega t - \delta), \text{where } A^2 = \frac{f_0^2}{(\omega_0^2 - \omega^2)^2 + 4\beta^2 \omega^2}$$